

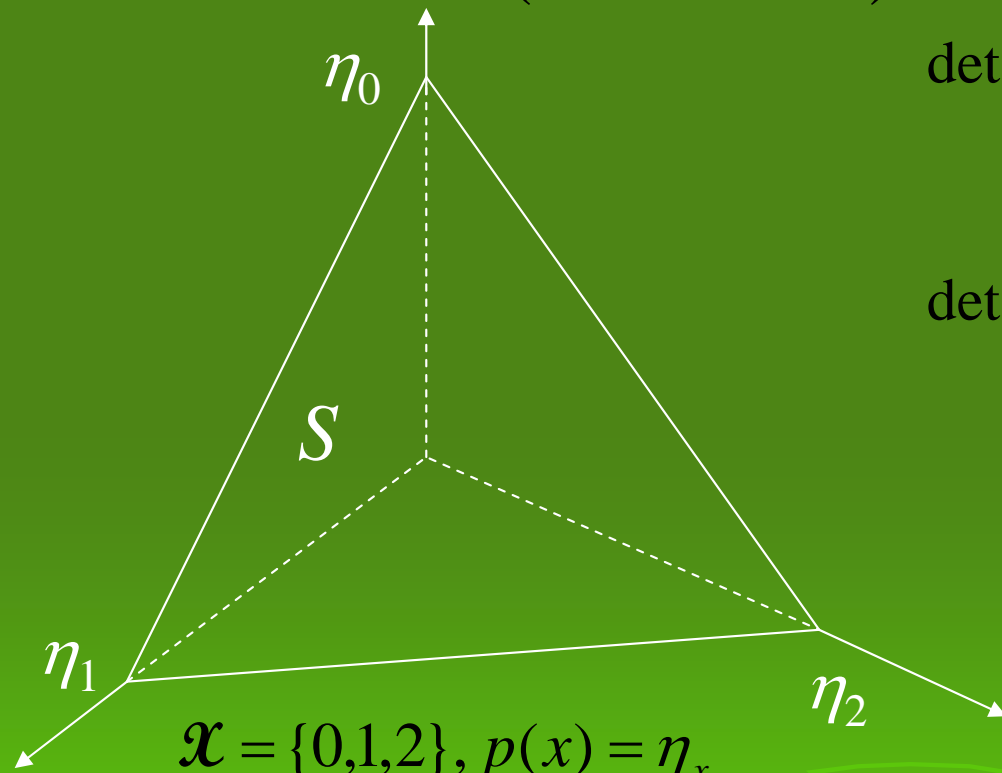
P61 定常Markovモデルの体積要素と 拡大モデルについて 竹内純一



Math-for-industry
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多項ベルヌーイモデルの場合

\bar{S} : 拡大モデル(非正規化)



$$\mathcal{X} = \{0,1,2\}, p(x) = \eta_x$$

$$\eta = (\eta_1, \eta_2) \text{ for } S$$

$$\eta = (\eta_0, \eta_1, \eta_2) \text{ for } \bar{S}$$

$$\det J = \begin{vmatrix} 1/\eta_1 + 1/\eta_0 & 1/\eta_0 \\ 1/\eta_0 & 1/\eta_2 + 1/\eta_0 \end{vmatrix} = \frac{1}{\eta_0 \eta_1 \eta_2}$$

$$\det \bar{J} = \begin{vmatrix} 1/\eta_0 & 0 & 0 \\ 0 & 1/\eta_1 & 0 \\ 0 & 0 & 1/\eta_2 \end{vmatrix} = \frac{1}{\eta_0 \eta_1 \eta_2}$$

J : Fisher情報行列

S の体積要素(密度) $\sqrt{(\det J)}$

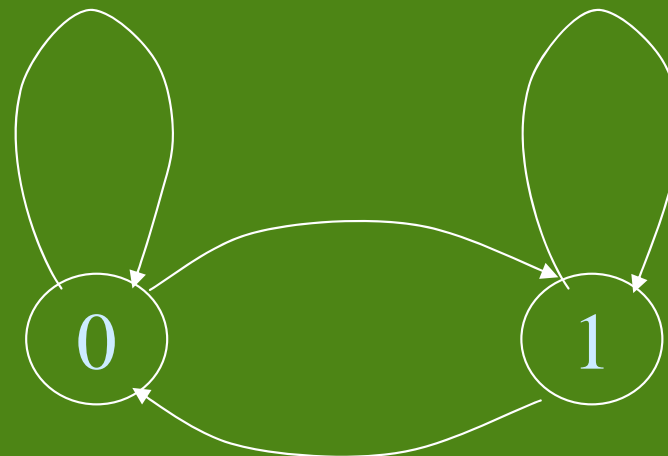
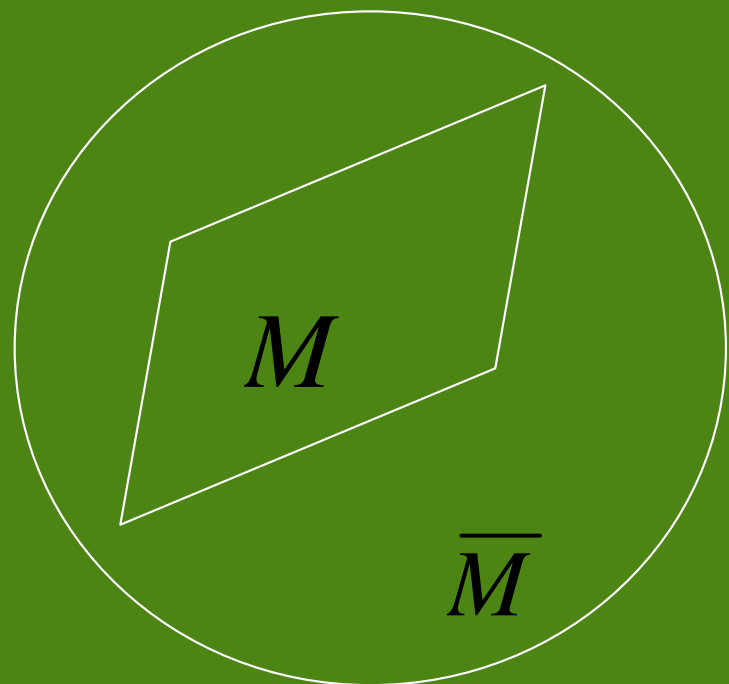
S のJeffreys事前分布 $w(\eta) \propto \sqrt{(\det J)}$

なぜ $\det J = \det \bar{J}$ か？



マルコフ連鎖モデルの場合

2状態の例



$$\mathcal{X} = \{0,1\}$$

$$\eta = (\eta_{00}, \eta_{10})$$

$$\bar{\eta} = (\eta_{00}, \eta_{01}, \eta_{10}, \eta_{11})$$

$$\det J = \left(\sum_{x \in \mathcal{X}} \Delta_{xx} \right)^2 \prod_{x \in \mathcal{X}} \frac{\eta_x}{\prod_{y \in \mathcal{X}} \eta_{xy}}$$

$$\det \bar{J} = 0$$

[Takeuchi 2009]

拡大モデルでは
 \bar{J} が退化する